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# Information cascades and the distribution of economic recessions in capitalist economies

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## Abstract

We consider in this paper the distribution of the cumulative size of recessions in 17 capitalist countries over the period 1871–1994, using data on annual percentage changes in real GDP. A recession is defined as a year in which GDP growth is negative, and the cumulative change is the change from peak to trough during a recession period. We examine both the whole sample and different partitions of the data.

The null hypothesis that the size distribution of recessions follows an exponential distribution is never rejected at the conventional level of statistical significance,  $p=0.05$ . However, there are always a small number of large recessions, no matter how the data is partitioned, which are not well fitted by a least-squares regression of the log of size on the rank of size. In other words, in a qualitative sense we see a bimodal distribution of recessions, with an exponential fit to the bulk of the data, and a second peak describing a small number of very large recessions.

A previously published agent-based economic theory model of the business cycle, calibrated purely on US data, is able with no change in its parameters to generate an exponential distribution of the size of recessions very close to that which is actually observed. In this model, information flows between agents on a completely connected network.

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## 1. Introduction

The phenomenon of information cascades [1] is widely observed in economic and social systems. Ref. [2] notes that small initial shocks can cascade to affect or disrupt

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1 large systems that have proved stable with respect to similar disturbances in the past.  
2 Examples include financial markets [3], the commercial success or failure of films [4],  
3 and the diffusion of crime [5].

4 Watts [2] offers a general theoretical model of a possible explanation in terms of a  
5 sparse, random network of interacting agents whose decisions are determined by the  
6 actions of their neighbours according to a simple threshold rule. Two regimes are identified  
7 in which the network is susceptible to very large cascades that occur very rarely.  
8 When cascade propagation is limited by the connectivity of the network, a power law  
9 distribution of cascades is observed. But when the network is highly connected, the size  
10 distribution of cascades is bimodal, with an exponential tail at small cascade size and a  
11 second peak at the size of the entire system corresponding to a single global cascade.

12 The purpose of this paper is to present evidence on the distribution of the size  
13 of recessions in the advanced capitalist economies, which are obvious examples of a  
14 networked system. A theoretical model is described in which information flows between  
15 agents on a completely connected network, and which offers an initial explanation of  
16 the observed distribution.

## 17 2. The background

18 Firms in the economy are connected in two distinct ways. First, there are the tech-  
19 nological connections which arise from the need for companies in any particular sector  
20 to use as inputs into their production the outputs of other industries. An example is  
21 the motor vehicle industry, which uses materials produced by other industries to make  
22 cars and trucks. Input–output tables in the national economic accounts describe these  
23 connections at the level of the industry.<sup>1</sup> Ref. [6] shows that in a modern developed  
24 economy, the connections between industries are rather extensive.

25 The second type of connection arises from the impact on any given firm of the  
26 decisions and opinions about the future of other firms in the economy. Keynes [7], for  
27 example, attached considerable importance to the state of long term expectations, or  
28 sentiment, for the decisions by companies to invest. The more optimistic the overall  
29 climate of opinion, the more likely it is that a firm will carry out an investment  
30 decision. Information about the general climate of expectations is readily available  
31 from the media, through newspapers such as the *Wall Street Journal*, for example.  
32 This is certainly the case as far as large companies are concerned. In other words, it is  
33 as if all agents are connected to, say, Microsoft or General Motors in terms of gathering  
34 information about the business climate. The information they gather may not be perfect,  
35 but a large amount of it is available.

36 So on both the technological and informational criteria, capitalist economies appear  
37 to be highly connected.

## 3. The data

38 Annual percentage changes in real GDP in 17 capitalist economies from 1871 to  
39 1994 are available from Ref. [8]. The individual countries are Australia, Austria,

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<sup>1</sup> Similar data are not available at the level of the firm.

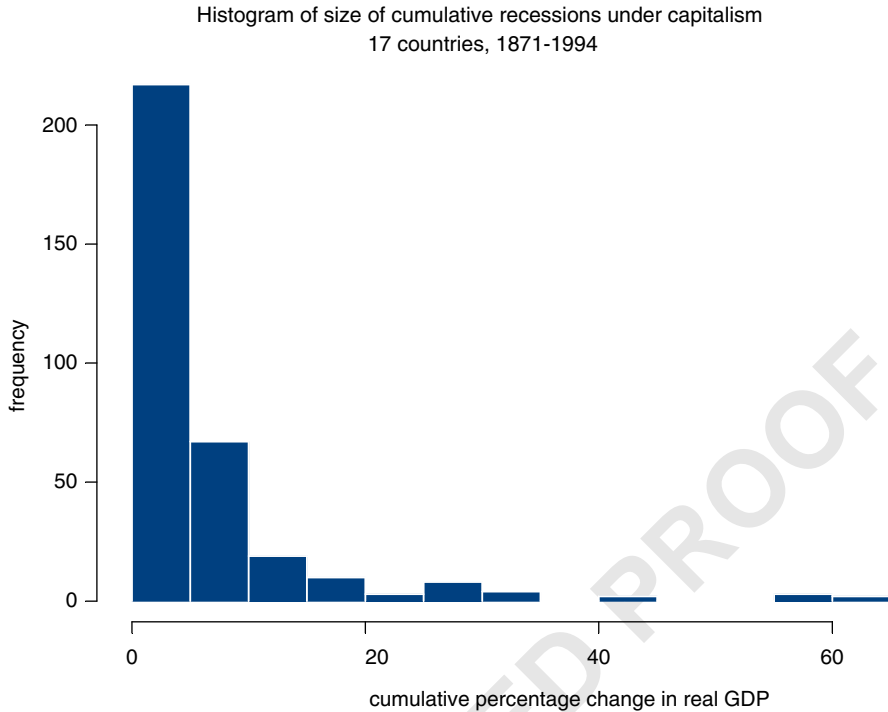


Fig. 1. Histogram of cumulative absolute fall in real GDP from peak to trough, 336 recessions in 17 capitalist countries 1871–1994.

1 Belgium, Canada, Denmark, France, Finland, Germany, Italy, Japan, Netherlands,  
2 New Zealand, Norway, Sweden, Switzerland, the UK and the US.<sup>2</sup>

3 There are formidable problems involved in constructing such data series, many of  
4 which are discussed in Ref. [8]. It is important for readers with a natural science  
5 background to appreciate that, outside financial markets, almost all economic data is  
6 estimated and the margin of error around any individual data point can be substantial.  
7 This is the case even with modern estimates of data for the most recent years.

8 Recessions can be measured in a number of ways. An unequivocal and widely  
9 accepted way of doing so is to define a recession as being a period of at least 1 year  
10 (given that annual data is being used<sup>3</sup>) in which the rate of growth of real GDP is  
11 less than zero. Across the 17 countries, we find 336 examples of recessions over the  
12 1871–1994 period.

13 In this paper, we analyse the cumulative size of recessions. In other words, the  
percentage change in real GDP from peak to trough. The size of recessions has varied

<sup>2</sup> Data for Japan is only available from 1886 and for Switzerland from 1901.

<sup>3</sup> Data at a higher frequency such as quarterly does not exist for periods before World War Two, and is only gradually available across the countries since then.

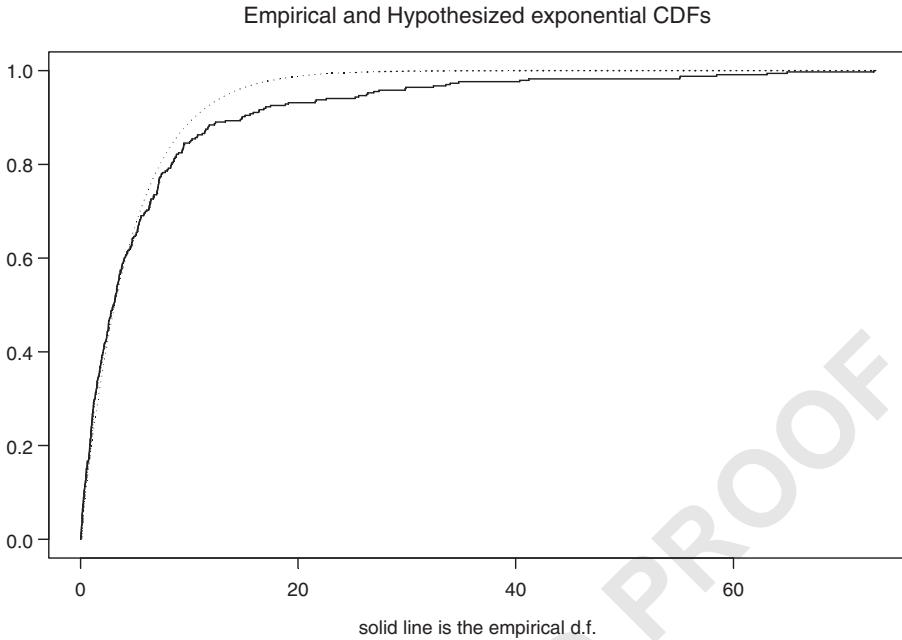


Fig. 2. Empirical distribution function of cumulative size of recessions (solid line) and hypothesized exponential cumulative distribution function with rate=0.22.

1 dramatically, from recessions in which output hardly fell at all to a few in which it  
 2 fell by more than 50 per cent. We use the absolute value of that data, for ease of  
 3 exposition (Fig. 1).

4 Most recessions have been small, with 81 out of the total of 336 observations having  
 5 a value of less than 1 per cent. There have been a small number of catastrophic falls,  
 6 with 12 observations being over 30 per cent. Most of these relate to the end and  
 7 immediate aftermath of war in the defeated countries in the world wars, but Canada  
 8 and the United States both experienced falls of over 30 per cent in the Great Depression  
 9 of the 1930s.

#### 4. Results

11 Fig. 2 compares the empirical distribution function of the sample with a hypothesized  
 12 cumulative distribution function which is an exponential with rate parameter=0.22.

13 On a formal Kolmogorov–Smirnov test, the null hypothesis that the data are dis-  
 14 tributed exponentially with rate=0.22 is rejected at  $p = 0.092$ . In other words, the null  
 15 hypothesis is not rejected at the standard level of statistical significance  $p = 0.05$ . This  
 16 rate, and the other empirically calibrated ones described below, was chosen by obtain-  
 17 ing an initial calibration by means of a plot as in Fig. 2, and then searching around  
 18 the neighbourhood of the initial rate in steps of 0.01 and choosing the rate at which  
 19 the  $p$ -value is maximised.

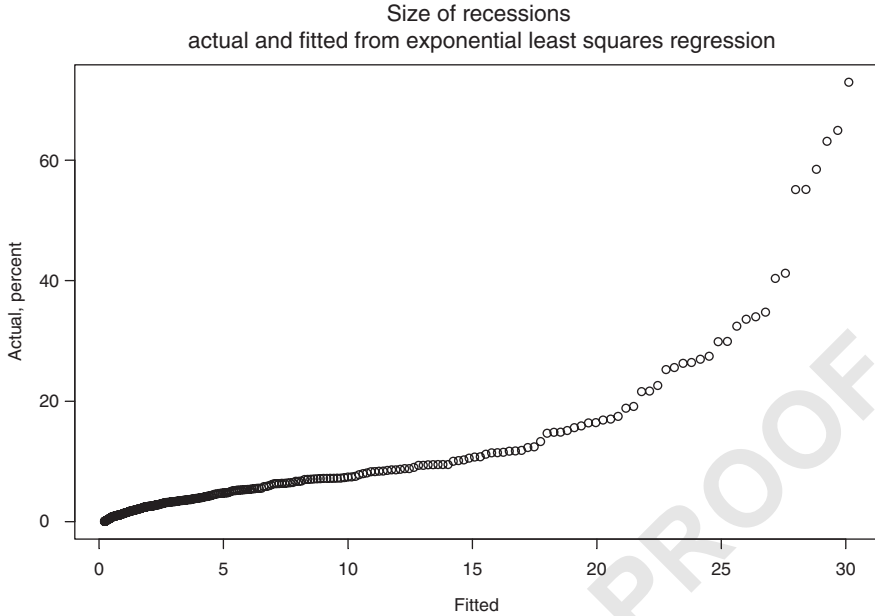


Fig. 3. Actual size of recessions and values fitted from exponential least-squares regression of log of size on rank. The relationship up to around values of 20 is described by a 45° line, but the large values are clearly outliers.

1 However, it is the bulk of the data which is essentially described by an exponential,  
 2 and the tail is fitted quite poorly. In the actual data, there are 313 out of the total  
 3 of 336 observations with a value of less than 20, and 308 in the values fitted by a  
 4 least-squares exponential fit to the rank of the data. However, the maximum value  
 5 predicted by the regression is 30.1, and we noted previously that there are 12 actual  
 6 observations above this level.

7 Excluding the observations with values above 20 makes little difference to the esti-  
 8 mated coefficient on the cumulative size. Using the whole sample it is 0.0147 with an  
 9 equation standard error of 0.374 and excluding the observations with values above 20  
 10 it is 0.0142 with an equation standard error of 0.367.

11 In other words, the bulk of the data is fitted well by an exponential relationship  
 12 between size and rank of size, but there is evidence of a bimodal distribution with a  
 13 small number of very large recessions being outliers. This is summarised in Fig. 3.

14 Most of the very large observations refer to the collapse of output in some occupied  
 15 countries in World War Two, and the defeated countries at the end of both world wars.  
 16 The sample was therefore divided into two groups, which for descriptive purposes we  
 17 refer to as 'allies' and 'rest'. The former group comprises those countries which were  
 18 neither defeated nor occupied during the world wars, plus the neutral countries of  
 19 Sweden and Switzerland. In other words, Australia, Canada, New Zealand, Sweden,  
 20 Switzerland, the UK and the US. The rest are in the 'rest' group.<sup>4</sup>

<sup>4</sup> This is not to suggest that France, for example, did not at some point fight against Germany, but it was occupied.

Table 1  
Size of cumulative recessions 1871–1994, absolute per cent, allied countries and the rest

	Min.	1st quartile	Median	3rd quartile	Max.
Allied	0.04	1.4	3.2	7.0	40.4
Rest	0.03	1.0	2.6	7.3	72.9

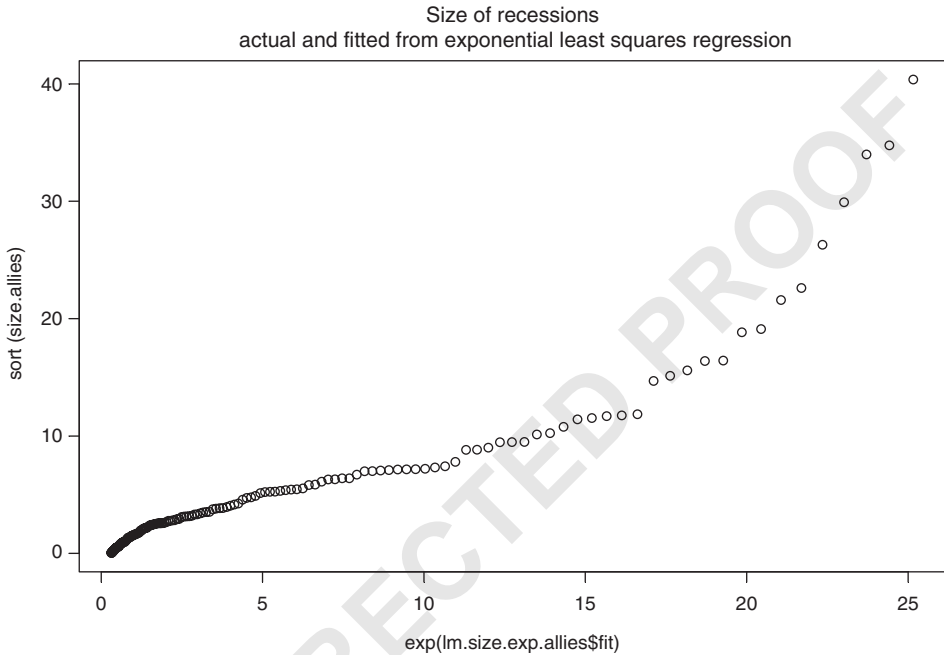


Fig. 4. Actual size of recessions and values fitted from exponential least-squares regression of log of size on rank, allied group of countries. The relationship up to around values of 20 is described by a 45° line, but the large values are clearly outliers.

1 There are 149 observations in the ‘allies’ group and 187 in the ‘rest’ group. The  
 2 bulk of the distribution of the data in these two groups is very similar (Table 1).

3 On a formal Kolmogorov–Smirnov test, the null hypothesis that the two distributions  
 4 are the same is rejected at  $p = 0.071$ , above the conventional level of significance at  
 5  $p = 0.05$ .

6 However, it is in the tail of the distributions where the experience of the two sets  
 7 of countries differ. The allies group has only 7 observations above 20 per cent with a  
 8 mean value of 29.9, and the rest group has 16 such observations with a mean value  
 9 of 41.1.

10 In neither case can the null hypothesis that the data are distributed exponentially be  
 11 rejected. With the allied group, a rate of 0.22 is only rejected at  $p = 0.77$ , although

Table 2  
Size of cumulative recessions, absolute per cent, 1871–1994 and 1950–1994

	Min.	1st quartile	Median	3rd quartile	Max.
1871–1994	0.03	1.0	3.1	7.1	72.9
1950–1994	0.03	0.5	1.5	2.9	14.8

1 for the rest a rate of 0.25 is rejected at  $p = 0.053$ , so this is much closer to rejection  
on conventional criteria.

3 Fig. 4 plots the allied group actual values and those fitted from a least-squares  
regression of the log of size against rank. The extreme values in the tail for this group  
5 do not arise from war-related events, such as the physical destruction of much of the  
capital stocks of Germany and Japan in 1945. But it is clear that even in this group,  
7 there are a small number of observations in the tail which are not described well by  
an exponential fit to the data.

9 Another way of examining the data is to divide the sample into pre- and post-World  
War Two, or more precisely from 1950, when the immediate economic impact of the  
11 war had faded and pre-war living standards had been surpassed in almost all countries.<sup>5</sup>  
In general, the variability of output growth from year to year has been less in the latter  
13 than in the former period. The standard deviation of the annual percentage change in  
real GDP across the 17 countries from 1871 to 1949 is 6.72, from 1871 to 1939 it is  
15 5.10. But from 1950 to 1994 it is 2.86. Table 2 compares the post-1950 experience  
with that of the full sample.

17 Fig. 5 compares the empirical distribution function of the 1950–1994 sample with  
a hypothesised cumulative distribution function which is an exponential with rate  
19 parameter=0.42.

The null hypothesis that the data are exponentially distributed is only rejected at  
21  $p = 0.73$  on a Kolmogorov–Smirnov test. There is, however, an outlying observation,  
relating to the recession in Finland in the early 1990s when output fell by almost 15  
23 per cent (Fig. 6).

Finally, we can consider the size distribution of recession according to their dura-  
25 tion. There is a number of ways in which the distribution of duration of recessions can  
be described [9–11], none of which are completely conclusive, given that the longest  
27 recession observed lasts for only 7 years. Fig. 7 plots the relationship between cumu-  
lative size and duration of recessions.

29 Overall, there is a positive correlation between the two of 0.58. But clearly, even in  
short recessions, falls in output can be very considerable. The null hypothesis that the  
31 size follows an exponential distribution cannot be rejected for recession lasting 1, 2, 3  
and more than 3 years, although the rate parameters differs between them (Table 3).

33 For recessions lasting both 1 and 2 years, the same problem regarding the fit of  
an exponential to the tail remains. The bulk of the data is fitted well, but there is in  
35 each case a small number of large outlying observations. One and two year durations

<sup>5</sup> Except Germany and Japan, which reached 1938 living standards in 1953.

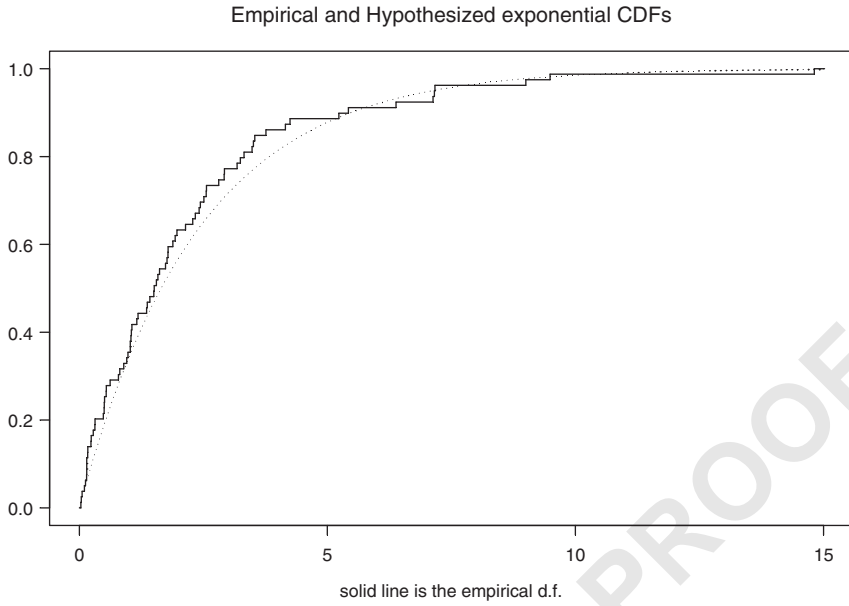


Fig. 5. Empirical distribution function of cumulative size of recessions 1950–1994 (solid line) and hypothesised exponential cumulative distribution function with rate=0.42.

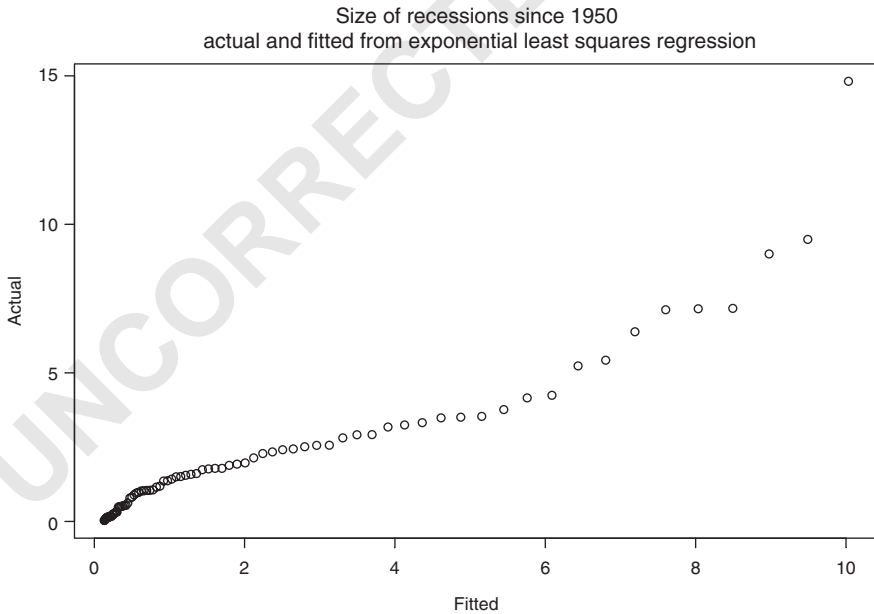


Fig. 6. Actual size of recessions and values fitted from exponential least-squares regression of log of size on rank, 17 capitalist countries, 1950–1994.







1 The model is completed by the equation describing how each agent determines its level of sentiment:

3 The sentiment of the  $i$ th agent is determined by the following:

$$y_i(t) = (1 - \beta)y_i(t - 1) - \beta[X(t - 1) + \eta_i(t)], \quad (2)$$

5 where  $X$  is the overall rate of growth of output of the economy (the weighted sum of the  $x_i$ ), and where  $\eta_i$  is drawn from a normal distribution with mean zero and standard deviation  $sd_2$ . The coefficient on  $X(t - 1)$ ,  $\beta$ , has a negative sign, again reflecting the Keynesian basis of the model [12, Chapter 22].

7 The coefficients calibrated against US data,  $\beta$ ,  $sd_1$  and  $sd_2$  were left unchanged. The only change made was to set the mean value of the output of the model at 2.0, which is the average annual real growth rate across all capitalist economies 1871–1994, instead of the 3.3 which is the growth rate of the US economy.

9 The model was run for 30,000 steps, which generated 4317 recessions. In the actual data, there are 2074 observations and 336 recessions. The proportions of recessions to total observations are 0.144 for the model and 0.162 for the actual data. Even using the model parameters calibrated on US data, the model is able to describe the range of the bulk of the data well. The 1st quartile, mean and 3rd quartiles of the actual data are, respectively,  $-0.1$ ,  $2.0$  and  $4.4$ . The model generates  $-0.1$ ,  $2.0$  and  $4.1$ . However, the extreme values, both in recession and in recoveries (almost exclusively after wars), of the actual data are not captured by the theoretical model.

11 The null hypothesis that the distribution of the size of the 4317 recessions generated by the model follows an exponential distribution is only rejected at  $p = 0.77$  on a Kolmogorov–Smirnov test. However, the rate parameter which gives this is 0.26, compared to the 0.22 of the actual data. The null hypothesis that the model output and the actual data follow the same distribution is rejected at  $p = 0.006$ .

13 Most of the very large recessions which are observed relate to periods either during or at the end of the two world wars. In the theoretical model above, the cycle is endogenous. In other words, it arises from the internal properties of the model and does not rely on the existence of external shocks. We might plausibly regard large scale destruction of domestic capital stock by enemy action as an external shock.

15 We therefore introduced downward external shocks to output (but not directly to sentiment) which, unlike  $\varepsilon_i(t)$ , are common to all agents in the period in which they occur. The actual data covers some 120 years, in the course of which there have been two periods of serious external shock to some, but not all, economies. The shocks are introduced every 60 steps and last for a single step each time. The size is drawn from a uniform distribution on  $[-20, -30]$ . The parameters  $sd_1$  and  $sd_2$  were re-calibrated slightly to 0.032 and 0.42 so that the output of the model continued to match the range of the bulk of the data between the first and third quartiles. The external shocks generated cumulative recessions of over 40 per cent fall in output.

17 With the model adjusted in this way, the null hypothesis that the actual size distribution of recessions is the same as the model generated distribution is not rejected at  $p = 0.11$  on a Kolmogorov–Smirnov test.

19 So this simple model, using parameters calibrated purely on US data, is able to replicate qualitatively the size distribution of recessions in 17 capitalist economies.

1 A refinement, to take account more explicitly of the idea in Ref. [2], would be to  
2 introduce sparsity into the connections between agents in terms of how they set their  
3 individual output growth. At present, each agent takes account of the sentiment of all  
4 other agents. Perhaps more realistically, agents will take particular account of agents in  
5 their own or related industries, and less account of agents operating in different sectors  
6 of the economy.

## 7 6. Conclusion

8 We consider in this paper the distribution of the cumulative size of recessions in  
9 17 capitalist countries over the period 1871–1994, using annual percentage changes  
10 in real GDP. A recession is defined as a year in which GDP growth is negative,  
11 and the cumulative change is the change from peak to trough during a recession  
12 period.

13 We examine different partitions of the data. We divide the sample into the victo-  
14 rious plus neutral countries in the world wars, and the rest. Very large output falls  
15 characterise many of the occupied and defeated countries. The overall variability of  
16 output growth has been much less since 1950, and we consider the distribution of  
17 the post-1950 recessions. And we examine the distribution of recessions of different  
18 duration.

19 The null hypothesis that the size distribution of recessions follows an exponential  
20 distribution is never rejected at the conventional level of statistical significance,  $p=0.05$ .

21 An agent-based economic theory model, previously published and calibrated against  
22 US real GDP growth data [12], generates an exponential size distribution of recessions,  
23 although the rate parameter is slightly different from the data across the 17 capitalist  
24 economies. In the model, the rate of growth of output of each agent is determined  
25 simply by the overall level of sentiment about the future held by all agents. In other  
26 words, it is as if the agents are on a fully connected network across which information  
27 flows. Each agent takes account of the sentiment of all other agents.

28 Although the null hypothesis that the size distribution of recessions follows an expo-  
29 nential distribution is not rejected, there are always a small number of large recessions,  
30 however the data is partitioned, which are not well fitted by a least-squares regression  
31 of size on the rank of size. In other words, in a qualitative sense we see a bimodal  
32 distribution of recessions, with an exponential fit to the bulk of the data, and a second  
33 peak describing a small number of very large recessions.

34 Ref. [2] describes a general theoretical model with no explicit economic content  
35 of a random network of interacting agents whose decisions are determined by the  
36 actions of their neighbours according to a simple threshold rule. This suggests that  
37 when the network is highly connected, a bimodal distribution of cascades will be  
38 observed. There will be an exponential tail at small cascade size and a second peak  
39 at the size of the entire system corresponding to a single global cascade. This seems  
40 qualitatively similar to what is observed. A combination of Refs. [2,12] may enable  
41 a general explanation of recessions to be given which explains the facts even more  
42 closely.

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## References

- 3 [1] S. Bikhchandani, D. Hirshleifer, I. Welch, *J. Polit. Economy* 100 (1992) 992–1006.  
[2] D.J. Watts, *Proc. Nat. Acad. Sci.* 99 (2002) 5766–5771.
- 5 [3] A. Kirman, *Bank of England Quarterly Bulletin*, Bank of England, UK, 1995.  
[4] A.S. De Vany, W.D. Walls, *Econ. J.* 106 (1996) 1493–1514.
- 7 [5] P. Ormerod, C. Mounfield, L. Smith, *Non-linear Modelling of Crime in the UK*, Home Office Research Series, Home Office, London, UK, 2003.
- 9 [6] W. Cook, P. Ormerod, *Physica A* (2003), submitted for publication, pre-print available at [www.volterra.co.uk](http://www.volterra.co.uk).
- 11 [7] J.M. Keynes, *The General Theory of Employment, Interest and Money*, Macmillan, New York, 1936.  
[8] A. Maddison, *Monitoring the World Economy 1820–1992*, OECD, Paris, 1995.
- 13 [9] P. Ormerod, C. Mounfield, *Physica A* 293 (2001) 573.  
[10] I. Wright, *cond-mat/0311585*, 2003.
- 15 [11] M. Ausloos, J. Miskiewicz, M. Sanglier, *cond-mat/0403143*, 2004.  
[12] P. Ormerod, *Physica A* 314 (2002) 774–785.
- 17 [13] J.M. Keynes, *The General Theory of Employment*, Macmillan, New York, 1936.